

Active Wheel Camber Control

ME 102B – Final Project

Gurmehr Klair, Dawood Junaid, Feynman Barney

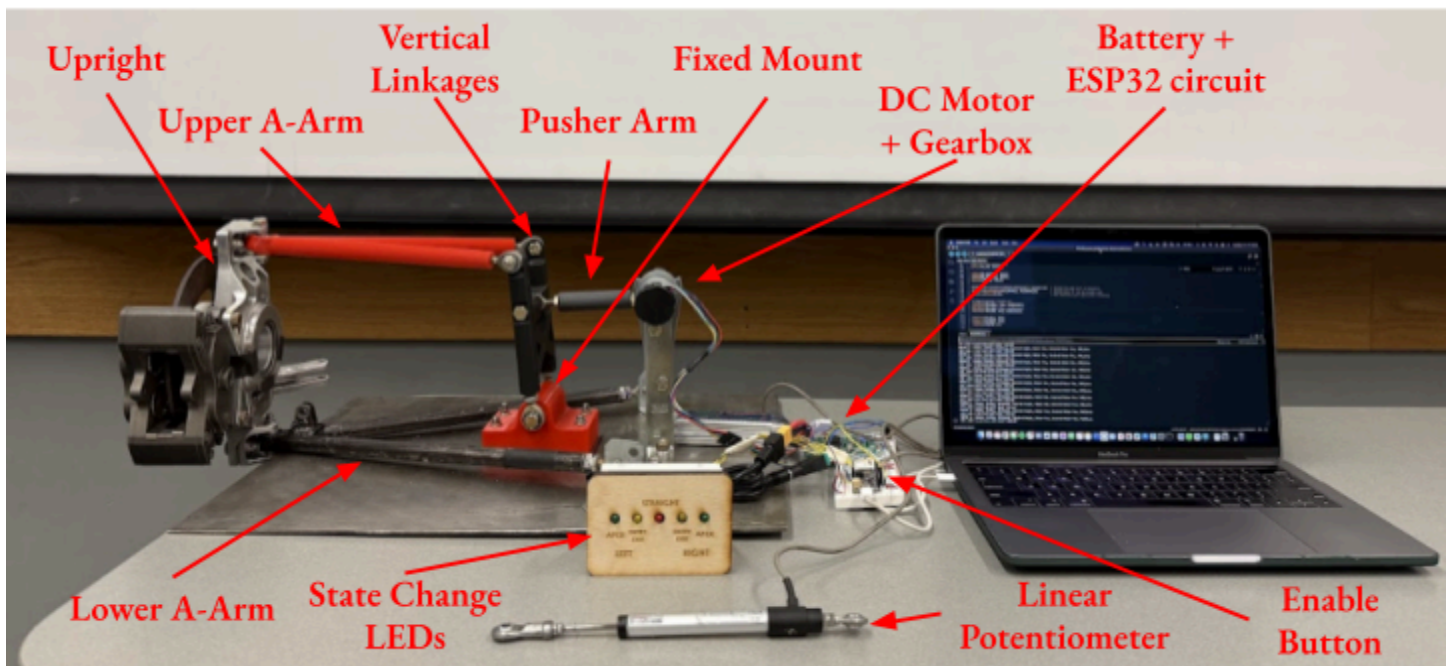
Opportunity

This project is a proof-of-concept mechanism developed with the Berkeley Formula Racing car in mind, to improve vehicle performance by reducing lap times and minimizing tire wear.

High-Level Strategy

We address this opportunity through an active wheel camber control mechanism. When viewed from the front or rear, Camber refers to the angle between a vehicle's vertical axis and the wheel. The ideal camber for straight-line acceleration is 0° to maximize the tire's longitudinal grip. However, some non-zero camber is required when the car is turning to compensate for the car rolling due to lateral load transfer. To maximize the tire's contact patch with the ground during a turn, negative camber is needed for the outside tire, while positive camber is necessary for the inside tire. Active camber control enables the individual tires to maintain optimal camber angles throughout different driving conditions on track, and this dynamic optimization allows the driver to navigate corners more quickly without compromising straight-line driving while evenly wearing the tires, ultimately improving overall performance. The original desired functionality was to control camber within the range of -5° and 5° within a half second of the steering input updating, and we achieved -6° and 6° within 0.8 seconds.

Integrated Physical Device

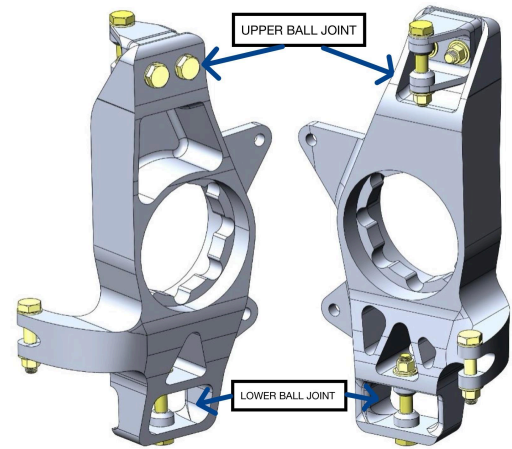


Function-Critical Decisions

The first step in function-critical calculations was a script that takes into consideration the different loads that the upright experiences in a real-life situation based on accelerometer data from the Formula SAE car. By taking moments and doing a force analysis, we were able to simplify the model to two compound cases that cause the greatest loads on our upper ball joint.

1. **Front_Compound_1:** Tight cornering with full-force braking.
2. **Front_Compound_2:** Tightest corner in FSAE competition combined with a worst-case bump.

The loads were applied in simulations to analyze force distribution between the **Upper Ball Joint (UBJ)** and **Lower Ball Joint (LBJ)**. Next, we used the maximum forces in each direction from the two different loadcases and used those forces for all further calculations.



To actuate the pivoting motion of the upright about the LBJ and counter forces acting on the UBJ, a motor was required to generate sufficient torque while meeting design constraints such as cost, efficiency, and response time. To achieve the required torque and speed, we selected a 12V brushed DC motor with a 131.25:1 metal gearbox and encoder with a resolution of 64 counts per revolution. It has a stalling torque of 45 kg-cm (4.41 Nm or 38.99 in-lbf). For the system to actuate quickly enough while the car is turning, we require the motor to turn 12 degrees in 0.5 seconds, or 4RPM. At this speed, the motor produces 34.76in-lbf. To ensure a load that is maximum 60% of the stalling torque, the motor should only provide 23.4in-lbf for actuation.

Force at Actuation Point (A)

Distance from pivot to actuation point = 0.8 in

Torque applied at actuation point = 23.4 in-lbf

$$F_A = \frac{\text{Torque}}{\text{Lever Arm}} = \frac{23.4 \text{ in-lbf}}{0.8 \text{ in}} = 29.25 \text{ lbf}$$

Force at Upper Ball Joint (Point C)

Distance from LBJ to UBJ = 6.5 in

Transfer arm distance = 3.94 in

$$F_C = \frac{F_A \times \text{Transfer Arm}}{\text{Lever Arm}} = \frac{29.25 \text{ lbf} \times 3.94 \text{ in}}{6.5 \text{ in}} = 17.72 \text{ lbf}$$

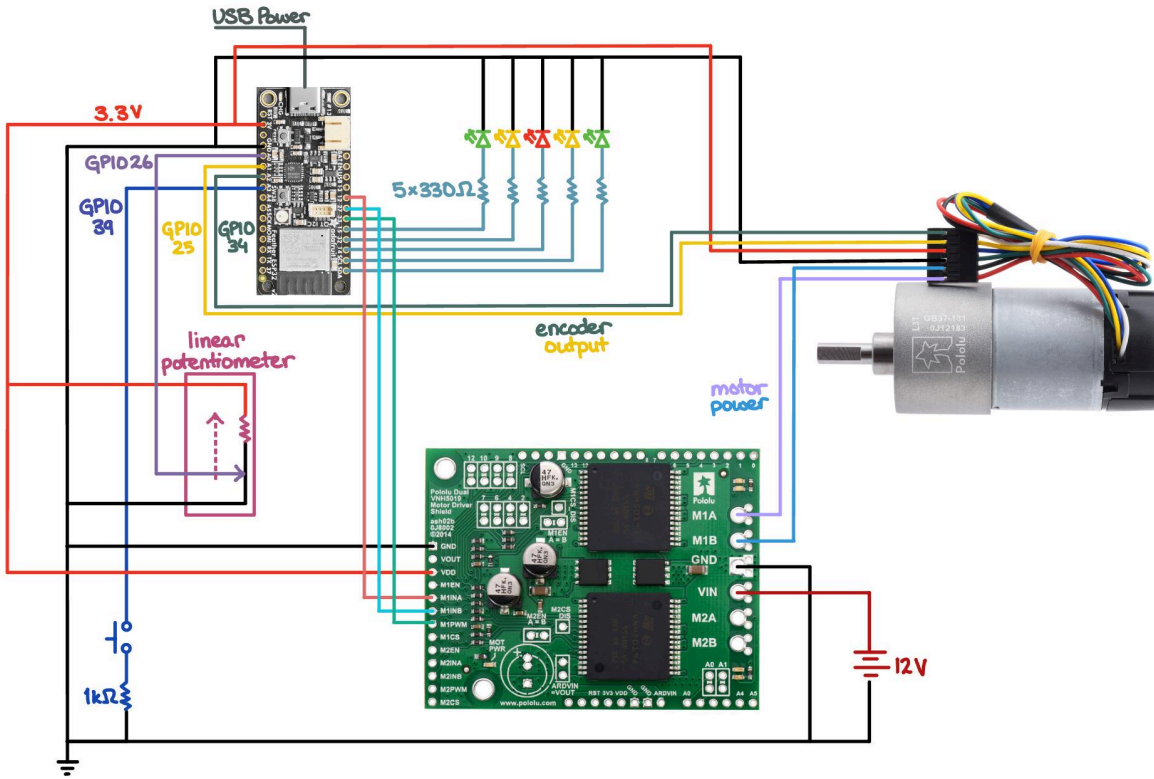
The simulated forces acting on the UBJ were resolved into a moment about the LBJ, providing the required torque. Based on how much force the motor can apply on the UBJ, we scaled down the force by a factor of 10, so that our effective lateral force is 12.2lbf while the motor applied 17.72lbf onto the UBJ with a 5.48lbf net force causing the upright to pivot along the fixed LBJ point. The forces in the other two directions will be resolved and triangulated onto the fixed points through the tubes.

We then were able to finalize material selection, concluding that the lower a-arm, rod-ends and mounts should be metal while the rest of the components could be 3D printed. Utilizing the new loads, we ran a simple FEA simulation to ensure that the parts were under a 3.5 factor of safety, due to the unreliable material properties of 3D-printed parts.

Reflection

In the initial stages of the project, our team was very excited about the project idea due to its novelty and potential to significantly improve the car's performance. However, the project turned out to be much more work than originally anticipated, and our initial mechanism design did not work out. We were able to adapt the project idea to simplify the components and manufacturing required, but it was an ongoing process to balance our ambitions for the project with time and cost constraints. If we were to do this project again, we would have started with a simpler prototype in the initial design phase and worked more closely during the integration phase.

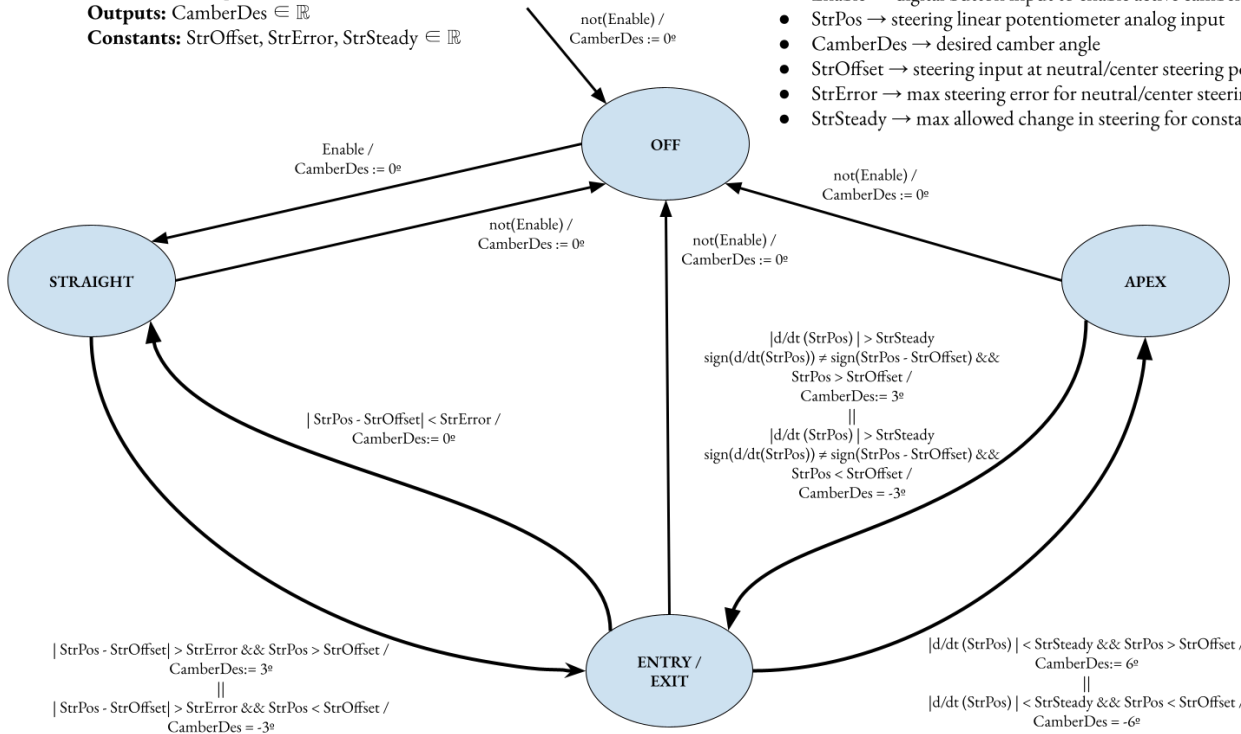
Circuit Diagram



State Transition Diagram

Inputs: Enable : pure, StrPos $\in \mathbb{R}$
Outputs: CamberDes $\in \mathbb{R}$
Constants: StrOffset, StrError, StrSteady $\in \mathbb{R}$

- Notes:**
- Enable → digital button input to enable active camber control
 - StrPos → steering linear potentiometer analog input
 - CamberDes → desired camber angle
 - StrOffset → steering input at neutral/center steering position
 - StrError → max steering error for neutral/center steering position
 - StrSteady → max allowed change in steering for constant steering



Front-Left Corner of the Car

- Steering left → steering input greater than StrOffset, inside tire
- Steering right → steering input less than StrOffset, outside tire

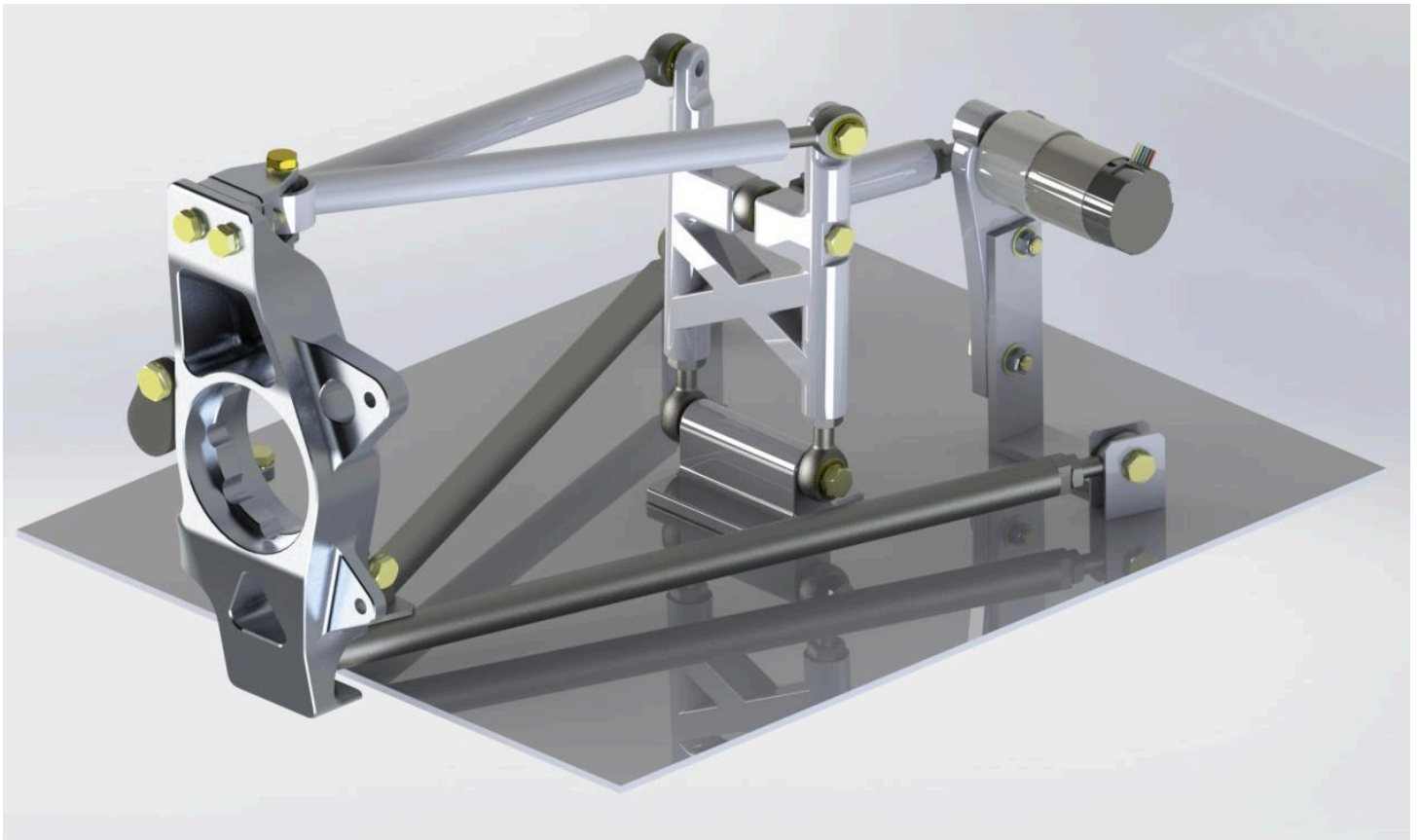
Appendix

Bill of Materials

Required Parts	Material/ Listing Name	Quantity	Cost	Supplier
Hardware				
Filament for Upper A-Arms	Standard Bambu Labs PLA	66.69 cc	\$ 1.67	Amazon
Filament for Vertical Linkage & Mount	Standard Bambu Labs PLA	174.59 cc	\$ 5.24	Amazon
Filament for Motor Linkage & Mount	Standard Bambu Labs PLA	37.7 cc	\$ 0.94	Amazon
Filament for Pushbar	Standard Bambu Labs PLA	5 cc	\$ 0.15	Amazon
Upright	Aluminum CNC'd Suspension Upright	1	\$ -	Berkeley Formula Racing
Tubes for Lower A-Arms	Welded Aluminum Tubing	1 set	\$ -	Berkeley Formula Racing
Ball Joints		2	\$ -	Berkeley Formula Racing
AN3 Bolts		14	\$ 24.00	Amazon
AN3 Washers		28	\$ 2.40	McMaster-Carr
AN3 KNuts		14	\$ 28.00	McMaster-Carr
Rod Ends		8	\$ -	Berkeley Formula Racing
L-brackets	Various sizes for mounting	3	\$ -	Berkeley Formula Racing
Mounting Plate	1/8" Steel Plate	1	\$ -	Berkeley Formula Racing
Electronics				
Motor	131:1 Metal Gearmotor 37Dx73L mm 12V with 64 CPR Encoder (Helical Pinion)	1	\$ 51.95	Pololu
Motor Driver	Pololu Dual VNH5019 Motor Driver Shield for Arduino	1	\$ 59.95	Pololu
2 Pack Battery & Charger	2 Pack XT60 Plug 12V 3S 2200mAh Lipo Battery and 1 Charger 12V 2200mAh XT60 2	1	\$ 39.99	Amazon
Battery Adapter	XT60 to DC5521 Power Cable, XT-60 Male to DC 5.5mm x 2.1mm Male Adapter Cord	1	\$ 9.99	Amazon
Linear Potentiometer	Texense Pulling Rod Linear Sensor	1	\$ -	Berkeley Formula Racing
ESP32	Huzzah Feather V2 ESP32	1	\$ -	Lab Kit
Button	Push Button	1	\$ -	Lab Kit
Resistors	330 & 1k Ohm resistors	6	\$ -	Lab Kit

LEDs	Red, yellow, green LEDs	5	\$ -	Lab Kit
Wires	Various	-	\$ -	Lab Kit
Total Cost			\$ 224.28	

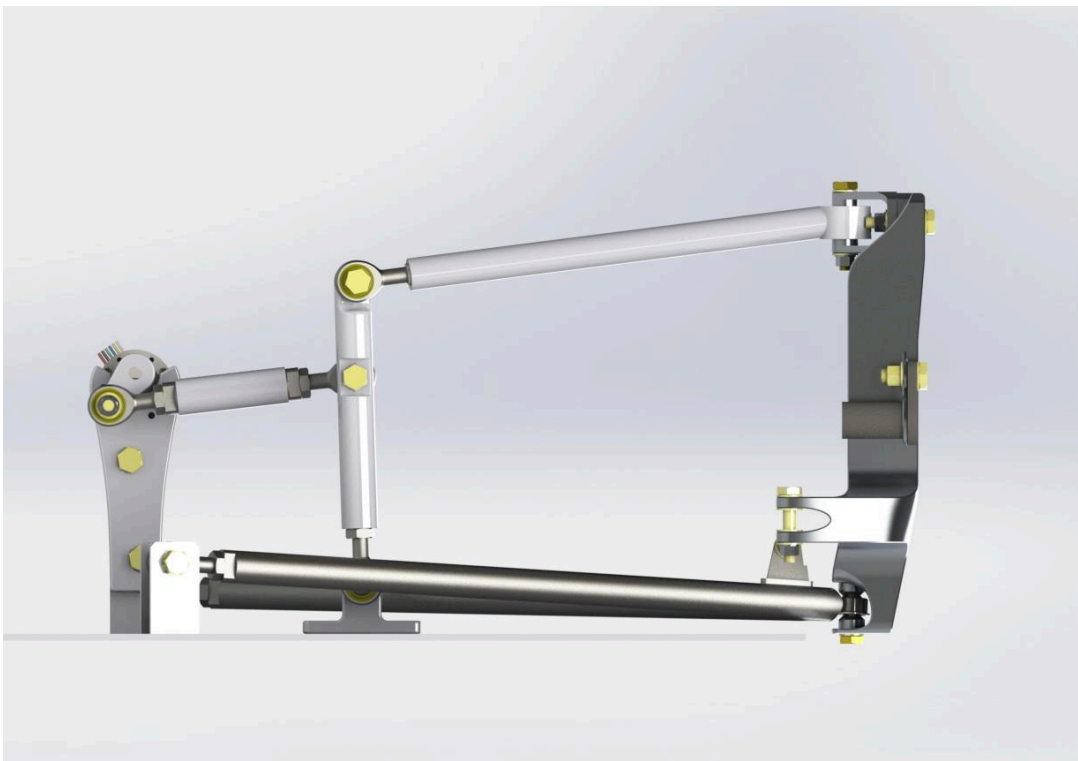
CAD Images



Isometric View



Top View



Front View

Code

```
ACC_Code_102B_Final.ino
1  #include <Arduino.h>
2  #include <ESP32Encoder.h>
3
4  #define M1_IN_A 12
5  #define M1_IN_B 27
6  #define M1_PWM 33
7  #define M1_SENSOR_A 25
8  #define M1_SENSOR_B 34
9  #define STR_POS 26
10 #define BTN 39
11 #define LED_RIGHT_GREEN 15
12 #define LED_RIGHT_YELLOW 32
13 #define LED_STRAIGHT_RED 14
14 #define LED_LEFT_YELLOW 20
15 #define LED_LEFT_GREEN 22
16
17 ESP32Encoder encoder;
18
19 // State Machine States
20 enum State {
21     OFF,
22     STRAIGHT,
23     ENTRY_EXIT,
24     APEX
25 } currentState = OFF;
26 bool ACC_Enable = false;
27
28 // Steering Constants & Variables
29 const int straightOffset = 2047;
30 const int maxStraightError = 750;
31 const double maxSteadyError = 70;
32 int strPos = 0;
33 const int windowSize = 5;
34 int strValues[windowSize];
35 double strSpeed = 0;
36
37 // Desired Camber Angles
38 double straightCamber = 0;
39 double eLeft = 3;
40 double eRight = -3;
41 double apexLeft = 6;
42 double apexRight = -6;
43 double camberAngle = straightCamber;
44
45 // Motor Variables
46 const int thetaMax = 8400; // encoder counts per 1 revolution of output shaft
47 int a = -120; // encoder ticks per angle // TODO
48 int b = 2048; // encoder ticks for zero // TODO
49 int theta = b;
50 int thetaDes = 0;
51 int error = 0;
52 int sumError = 0;
53 int lastError = 0;
54
55 double Kp = 0.4; // TODO
56 double Ki = 0.05;
57 double Kd = -0.05;
58 double X;
59
60 // Interrupt Variables
```

ACC_Code_102B_Final.ino

```
61 volatile bool buttonPressed = false;
62 int debounceDelay = 500; // ms
63 unsigned long lastButtonPressTime = 0; // To track button press time
64
65 volatile int count = 0;
66 volatile bool deltaT = false; // check timer interrupt
67 hw_timer_t* timer0 = NULL;
68 portMUX_TYPE timerMux0 = portMUX_INITIALIZER_UNLOCKED;
69 const int timerFreq = 1000000; // 1 us / 1MHz
70 const int alarmFreq = 100000; // 10,000 * 1 us = 10 ms
71
72 // PWM Properties
73 const int freq = 5000;
74 const int resolution = 8;
75 const int MAX_PWM_VOLTAGE = 255;
76 const int NOM_PWM_VOLTAGE = 150;
77
78 // Interrupt Services
79 void IRAM_ATTR isr_btn() { // the function to be called when interrupt is triggered
80     unsigned long currentMillis = millis();
81     if (currentMillis - lastButtonPressTime >= debounceDelay) {
82         buttonPressed = true;
83         lastButtonPressTime = currentMillis;
84     }
85 }
86
87 void IRAM_ATTR onTime0() {
88     portENTER_CRITICAL_ISR(&timerMux0);
89     count = encoder.getCount();
90     encoder.clearCount();
91     deltaT = true; // the function to be called when timer interrupt is triggered
92     portEXIT_CRITICAL_ISR(&timerMux0);
93 }
94
95 void setup() {
96     // Put your setup code here, to run once:
97     Serial.begin(115200);
98
99     pinMode(M1_IN_A, OUTPUT);
100    pinMode(M1_IN_B, OUTPUT);
101    digitalWrite(M1_IN_A, LOW); // Set initial state of motor to off
102    digitalWrite(M1_IN_B, LOW);
103    pinMode(M1_PWM, OUTPUT);
104
105    pinMode(M1_SENSOR_A, INPUT);
106    pinMode(M1_SENSOR_B, INPUT);
107    pinMode(STR_POS, INPUT);
108
109    ESP32Encoder::useInternalWeakPullResistors = puType::up; // Enable the weak pull up resistors
110    encoder.attachHalfQuad(M1_SENSOR_A, M1_SENSOR_B); // Attach pins for use as encoder pins
111    encoder.setCount(2048); // Set starting count value after attaching
112
113    // Attach channel to GPIO pin
114    ledcAttach(M1_IN_A, freq, resolution);
115    ledcAttach(M1_IN_B, freq, resolution);
116    ledcAttach(M1_PWM, freq, resolution);
117
118    ledcWrite(M1_IN_A, LOW);
119    ledcWrite(M1_IN_B, LOW);
120    ledcWrite(M1_PWM, 0);
```


ACC_Code_102B_Final.ino

```
121
122 // Set up button
123 attachInterrupt(BTN, isr_btn, RISING);
124
125 // Initilize timers
126 timer0 = timerBegin(timerFreq); // timer 0
127 timerAttachInterrupt(timer0, &onTime0); // edge (not level) triggered
128 timerAlarm(timer0, alarmFreq, true, 0); // autoreload enabled, infinite reloads
129
130 // Initialize steering values array
131 for (int i = 0; i < windowSize; i++) {
132     strValues[i] = 0;
133 }
134
135 // Initialize LED pins
136 pinMode(LED_RIGHT_GREEN, OUTPUT);
137 pinMode(LED_RIGHT_YELLOW, OUTPUT);
138 pinMode(LED_STRAIGHT_RED, OUTPUT);
139 pinMode(LED_LEFT_YELLOW, OUTPUT);
140 pinMode(LED_LEFT_GREEN, OUTPUT);
141
142 digitalWrite(LED_RIGHT_GREEN, HIGH);
143 digitalWrite(LED_RIGHT_YELLOW, HIGH);
144 digitalWrite(LED_STRAIGHT_RED, HIGH);
145 digitalWrite(LED_LEFT_YELLOW, HIGH);
146 digitalWrite(LED_LEFT_GREEN, HIGH);
147 delay(2000);
148
149 digitalWrite(LED_RIGHT_GREEN, LOW);
150 digitalWrite(LED_RIGHT_YELLOW, LOW);
151 digitalWrite(LED_STRAIGHT_RED, LOW);
152 digitalWrite(LED_LEFT_YELLOW, LOW);
153 digitalWrite(LED_LEFT_GREEN, LOW);
154 }
155
156 void loop() {
157     // put your main code here, to run repeatedly:
158     if (deltaT) {
159         portENTER_CRITICAL(&timerMux0);
160         deltaT = false;
161         portEXIT_CRITICAL(&timerMux0);
162
163         // Get steering angle and update array of last 10 steering values
164         strPos = analogRead(STR_POS);
165         for (int i = 0; i < (windowSize - 1); i++) {
166             strValues[i] = strValues[i + 1];
167         }
168         strValues[windowSize - 1] = strPos;
169         updateSteeringSpeed();
170
171         // State Machine Logic
172         switch (currentState) {
173             case OFF:
174                 camberAngle = straightCamber;
175                 if (CheckForButtonPress()) {
176                     currentState = STRAIGHT;
177                 }
178                 setLEDPIN(0);
179                 break;
180             case STRAIGHT:
```

ACC_Code_102B_Final.ino

```
181     if (!CheckIfStraight()) {
182         camberAngle = (TurningLeft()) ? eLeft : eRight;
183         currentState = ENTRY_EXIT;
184     }
185     if (CheckForButtonPress()) {
186         currentState = OFF;
187     }
188     setLEDPIN(3);
189     break;
190 case ENTRY_EXIT:
191     if (SteeringSteady()) {
192         camberAngle = (TurningLeft()) ? apexLeft : apexRight;
193         currentState = APEX;
194     }
195     if (CheckIfStraight()) {
196         camberAngle = straightCamber;
197         currentState = STRAIGHT;
198     }
199     if (CheckForButtonPress()) {
200         currentState = OFF;
201     }
202     if (TurningLeft()) {
203         setLEDPIN(4);
204     } else {
205         setLEDPIN(2);
206     }
207     break;
208 case APEX:
209     if (!SteeringSteady() && ReturningToStraight()) {
210         camberAngle = (TurningLeft()) ? eLeft : eRight;
211         currentState = ENTRY_EXIT;
212     }
213     if (CheckForButtonPress()) {
214         currentState = OFF;
215     }
216     if (TurningLeft()) {
217         setLEDPIN(5);
218     } else {
219         setLEDPIN(1);
220     }
221     break;
222 }
223
224 controlMotor();
225
226 plotControlData();
227 }
228 }
229
230 // Calculate Steering Speed
231 void updateSteeringSpeed() {
232     double sum = 0;
233     for (int i = 0; i < (windowSize - 1); i++) {
234         sum += double(strValues[i + 1] - strValues[i]) * (timerFreq / alarmFreq);
235     }
236     strSpeed = sum / (windowSize - 1);
237 }
238
239 // State Machine Checks
240 bool CheckForButtonPress() {
```

ACC_Code_102B_Final.ino

```
241     if (buttonPressed == true) {
242         buttonPressed = false;
243         return true;
244     } else {
245         return false;
246     }
247 }
248
249 bool CheckIfStraight() {
250     return (abs(strPos - straightOffset) < maxStraightError);
251 }
252
253 bool TurningLeft() {
254     return (strPos > straightOffset);
255 }
256
257 bool SteeringSteady() {
258     updateSteeringSpeed();
259     return (abs(strSpeed) < maxSteadyError);
260 }
261
262 bool ReturningToStraight() {
263     updateSteeringSpeed();
264     if (TurningLeft()) {
265         return (strSpeed < 0);
266     } else {
267         return (strSpeed > 0);
268     }
269 }
270
271 void controlMotor() {
272     // Update theta from encoder count delta
273     theta += count;
274     // Convert desired camber angle to desired theta
275     thetaDes = camberAngle * a + b;
276
277     // Control
278     error = thetaDes - theta;
279     sumError += error;
280
281     double P = Kp * error;
282     double I = Ki * sumError;
283     double D = Kd * (error - lastError);
284     X = P + I + D;
285
286     // Clip output & anti-windup
287     if (X > MAX_PWM_VOLTAGE) {
288         X = MAX_PWM_VOLTAGE;
289         sumError -= error;
290     } else if (X < -MAX_PWM_VOLTAGE) {
291         X = -MAX_PWM_VOLTAGE;
292         sumError -= error;
293     }
294
295     if (currentState == OFF) {
296         ledcWrite(M1_IN_A, LOW);
297         ledcWrite(M1_IN_B, LOW);
298         ledcWrite(M1_PWM, 0);
299         return;
300     }
301 }
```

ACC_Code_102B_Final.ino

```
301
302 // Map X to motor direction
303 if (X > 0) {
304     ledcWrite(M1_IN_A, LOW);
305     ledcWrite(M1_IN_B, MAX_PWM_VOLTAGE);
306     ledcWrite(M1_PWM, X);
307 } else if (X < 0) {
308     ledcWrite(M1_IN_A, MAX_PWM_VOLTAGE);
309     ledcWrite(M1_IN_B, LOW);
310     ledcWrite(M1_PWM, -X);
311 } else {
312     ledcWrite(M1_IN_A, LOW);
313     ledcWrite(M1_IN_B, LOW);
314     ledcWrite(M1_PWM, 0);
315 }
316 lastError = error;
317 }
318
319 void setLEDPIN(int led) {
320     switch (led) {
321         case 0:
322             digitalWrite(LED_RIGHT_GREEN, LOW);
323             digitalWrite(LED_RIGHT_YELLOW, LOW);
324             digitalWrite(LED_STRAIGHT_RED, LOW);
325             digitalWrite(LED_LEFT_YELLOW, LOW);
326             digitalWrite(LED_LEFT_GREEN, LOW);
327             break;
328         case 1:
329             digitalWrite(LED_RIGHT_GREEN, HIGH);
330             digitalWrite(LED_RIGHT_YELLOW, LOW);
331             digitalWrite(LED_STRAIGHT_RED, LOW);
332             digitalWrite(LED_LEFT_YELLOW, LOW);
333             digitalWrite(LED_LEFT_GREEN, LOW);
334             break;
335         case 2:
336             digitalWrite(LED_RIGHT_GREEN, LOW);
337             digitalWrite(LED_RIGHT_YELLOW, HIGH);
338             digitalWrite(LED_STRAIGHT_RED, LOW);
339             digitalWrite(LED_LEFT_YELLOW, LOW);
340             digitalWrite(LED_LEFT_GREEN, LOW);
341             break;
342         case 3:
343             digitalWrite(LED_RIGHT_GREEN, LOW);
344             digitalWrite(LED_RIGHT_YELLOW, LOW);
345             digitalWrite(LED_STRAIGHT_RED, HIGH);
346             digitalWrite(LED_LEFT_YELLOW, LOW);
347             digitalWrite(LED_LEFT_GREEN, LOW);
348             break;
349         case 4:
350             digitalWrite(LED_RIGHT_GREEN, LOW);
351             digitalWrite(LED_RIGHT_YELLOW, LOW);
352             digitalWrite(LED_STRAIGHT_RED, LOW);
353             digitalWrite(LED_LEFT_YELLOW, HIGH);
354             digitalWrite(LED_LEFT_GREEN, LOW);
355             break;
356         case 5:
357             digitalWrite(LED_RIGHT_GREEN, LOW);
358             digitalWrite(LED_RIGHT_YELLOW, LOW);
359             digitalWrite(LED_STRAIGHT_RED, LOW);
360             digitalWrite(LED_LEFT_YELLOW, LOW);
```

```
361     digitalWrite(LED_LEFT_GREEN, HIGH);
362     break;
363 }
364 }
365
366 void plotControlData() {
367     Serial.println("MOTOR 1 - State, StrPos, StrSpeed, Desired Angle, Motor Pos, Desired Motor Pos, PWM_Duty");
368     Serial.print(stateToString(currentState));
369     Serial.print(" ");
370     Serial.print(strPos - straightOffset);
371     Serial.print(" ");
372     Serial.print(strSpeed);
373     Serial.print(" ");
374     Serial.print(camberAngle);
375     Serial.print(" ");
376     Serial.print(theta);
377     Serial.print(" ");
378     Serial.print(thetaDes);
379     Serial.print(" ");
380     Serial.println(X);
381 }
382
383 const char* stateToString(State state) {
384     switch (state) {
385         case OFF: return "OFF";
386         case STRAIGHT: return "STRAIGHT";
387         case ENTRY_EXIT: return "ENTRY_EXIT";
388         case APEX: return "APEX";
389     }
390 }
```